

Quiz 1

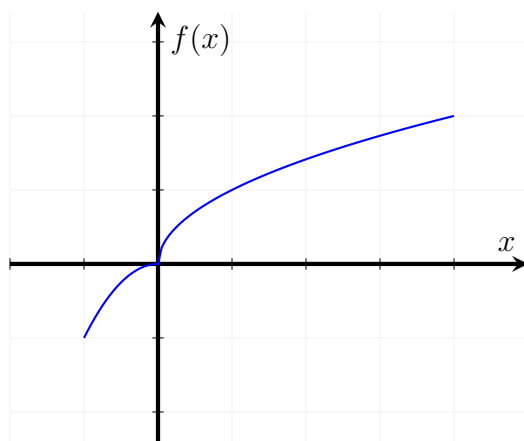
Note that $\mathbb{R} = (-\infty, \infty) =$ “all real numbers.”

1. Write down your major.
2. Let $f : \mathbb{R} \rightarrow \mathbb{R}$ and $g : \mathbb{R} \rightarrow \mathbb{R}$ be defined by the following rules:

$$f(x) = \log_2(x) + 2\log_2(3) - \log_2(5) \qquad g(x) = \log_2\left(\frac{9x}{5}\right)$$

Determine if the functions f and g are equal.

3. Let f be given by the following graphical representation:



Determine the following:

- (a) What type of function representation is this?
- (b) What is $f(1)$ and $f(-1)$?
- (c) What is the domain and range of f ?
- (d) Is this function one-to-one?
- (e) Is this function even, odd, both or neither?
- (f) When does $f(x) = 3$?
- (g) Is the function increasing, decreasing or neither on the interval $(0, 3)$?

Additional Exercises

1. Let $f : \mathbb{R} \rightarrow \mathbb{R}$ and $g : \mathbb{R} \rightarrow \mathbb{R}$ and determine if $f = g$ when,

(a)

$$f(x) = e^x e^{3-2x} + e^0 \qquad g(x) = e^{3-x}$$

(b)

$$f(x) = \cos(-x) - \tan(-x) \sin(x + 2\pi) \qquad g(x) = \sec(x)$$

2. Let $f : \mathbb{R} \rightarrow \mathbb{R}$ and $g : \mathbb{R} \rightarrow \mathbb{R}$, determine if fg is even, odd, both, or neither.
- (a) If f is even and g is even.
 - (b) If f is even and g is odd.
 - (c) If f is odd and g is even.
 - (d) If f is odd and g is odd.
3. Let $f : \mathbb{R} \rightarrow \mathbb{R}$ be a function, can f be both even and odd?
4. Let s be the side of a cube, determine the surface area and volume of the cube as a function of the side s .
5. Let s be the shorter side of a rectangle. Suppose that one side of the rectangle is twice the length of the other side. Determine the formula for the area and perimeter of the rectangle as a function of the side s .
6. Let $f : \mathbb{R} \rightarrow \mathbb{R}$ be defined by $f(x) = \sin(x)$, compute the following:
- (a) $f(0)$
 - (b) $f(\frac{\pi}{3})$
 - (c) $f(\frac{\pi}{4})$
 - (d) $2f(a)$
 - (e) $f(3a)$
 - (f) $f(-a)$
 - (g) $f(a+h)$
 - (h) $f(a^2)$
 - (i) $f(a)^2$